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# テアリング不安定性のジャイロ運動論シミュレーション

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2012 年 3 月 24 日

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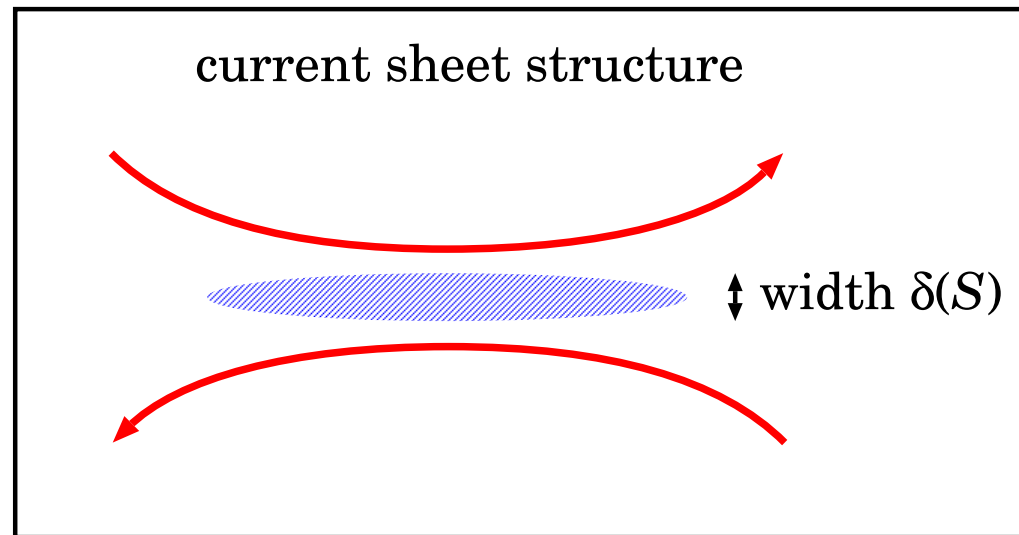
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# Magnetic reconnection is multiscale problem

Magnetic reconnection is  
▷ multiscale problem  
AstroGK: Astrophysical Gyrokinetics Code  
Collisions in AstroGK  
Problem setup  
Dispersion relation  
MHD to two-fluid MHD  
Collisional–collisionless transition  
Ion temp. dependence: kinetic Alfvén wave  
Summary

- Physics to break flux-freezing is necessary for field lines to change its topology: primarily by collisions (resistivity).  
⇒ Only collisions set a spatial scale in MHD model.
- Resistive spatial scale for weakly collisional plasmas falls below kinetic scales (MHD theory is not valid).
- Relevant kinetic scales:  $d_{i,e}$  [inertia],  $\rho_{i,e}$  [FLR],  $\rho_S$  [Sound].



# AstroGK: Astrophysical Gyrokinetics Code

Magnetic reconnection is multiscale problem

AstroGK:  
Astrophysical

▷ Gyrokinetics Code

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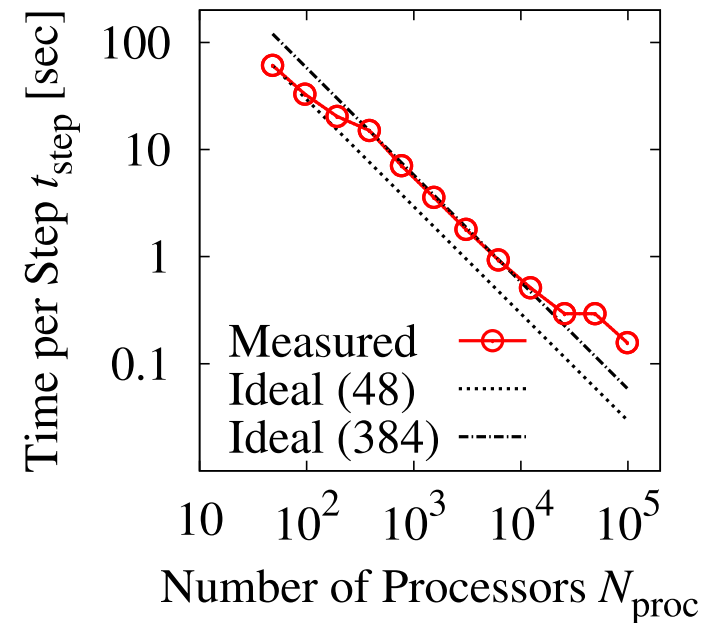
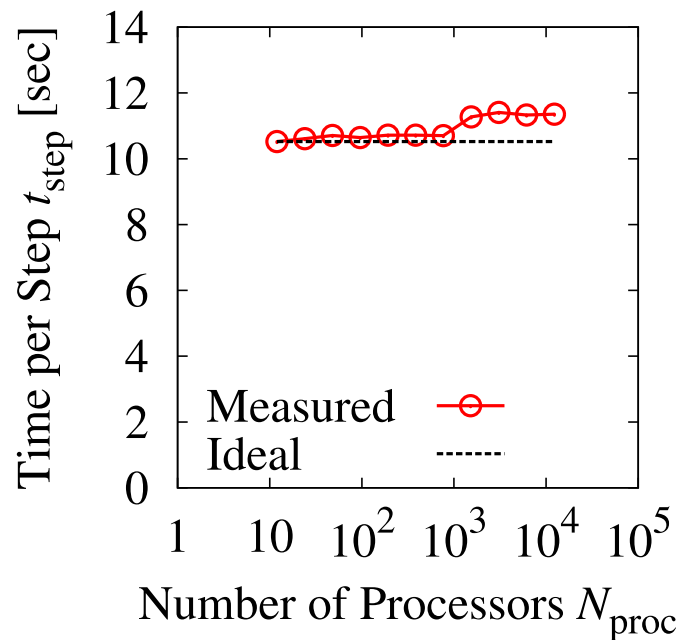
Ion temp. dependence: kinetic Alfvén wave

Summary

- Eulerian continuum, local flux tube,  $\delta f$ , electromagnetic code.
- Publicly available at <https://sourceforge.net/projects/gyrokinetics/>.
- Numata *et al.*, J. Comput. Phys. **229**, 9347 (2010).

Weak Scaling @ Kraken [Cray XT5]

Strong Scaling @ Kraken [Cray XT5]

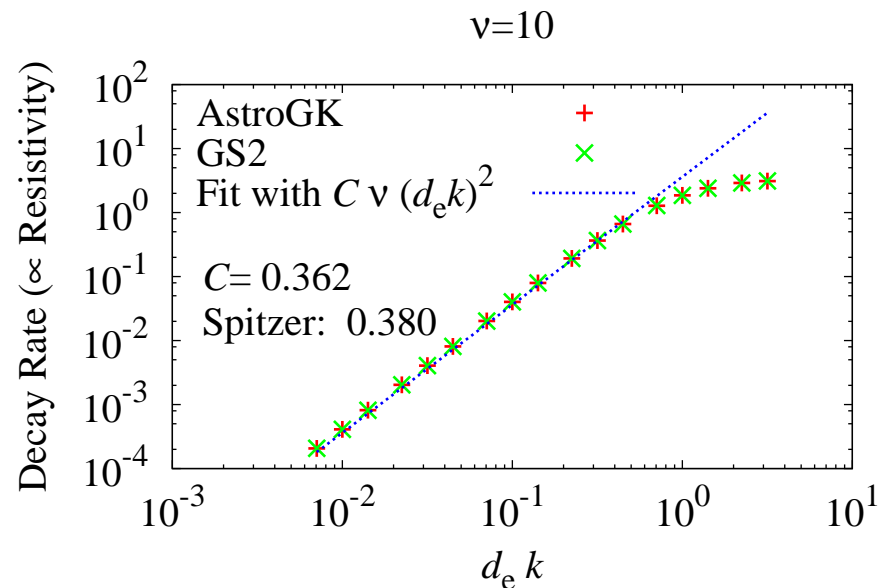


# Collisions in AstroGK

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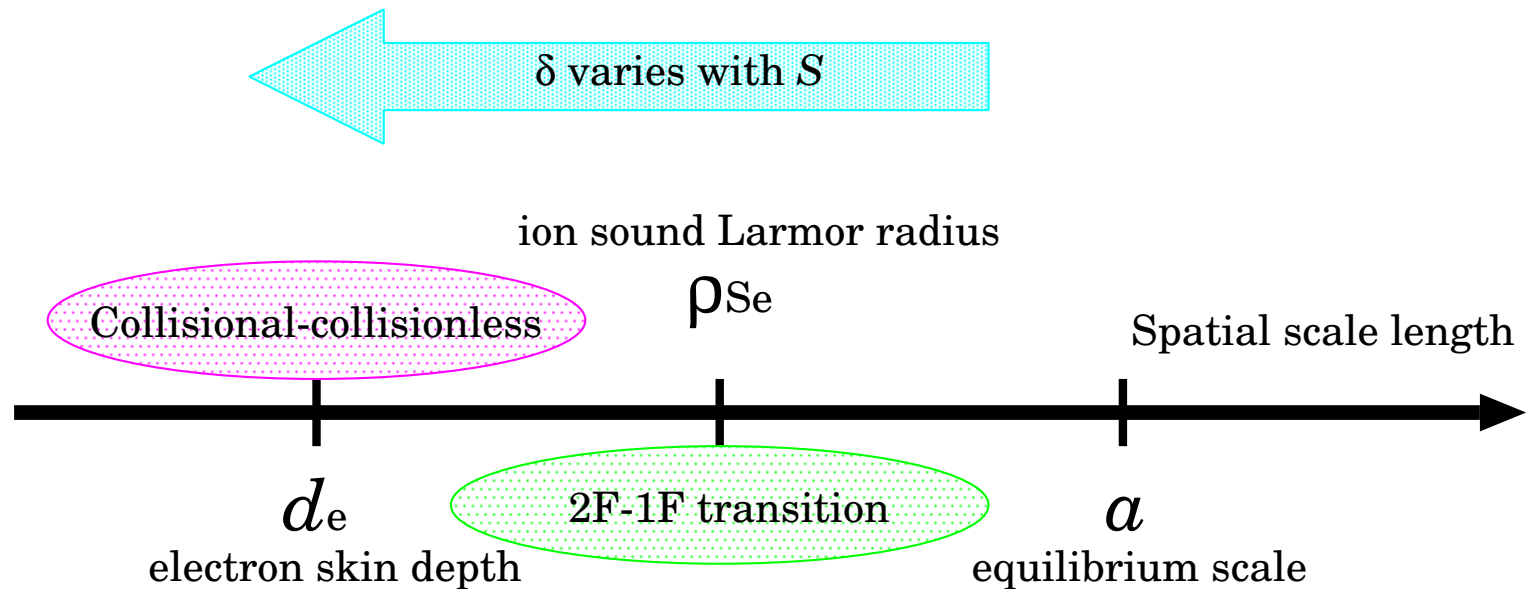
Recently, linearized collision operators for gyrokinetic simulations, which satisfies physical requirements are established and implemented in AstroGK [Abel *et al*, 2008; Barnes *et al*, 2009]

The operators are the pitch-angle scattering (Lorentz), the energy diffusion, and moments conserving corrections to those operators for like-particle collisions. Electron-ion collisions consists of pitch angle scattering by background ions and ion drag are also included.



# Problem setup

Collisionality  $\nu_e$  is scanned to vary current layer width  $\delta$ . As  $\nu_e$  is decreased, the current layer width becomes narrower, and the ion and electron kinetic scales become important.



**Case 1** electron scale  $\ll$  ion scale  $\sim \delta \ll$  equili. scale

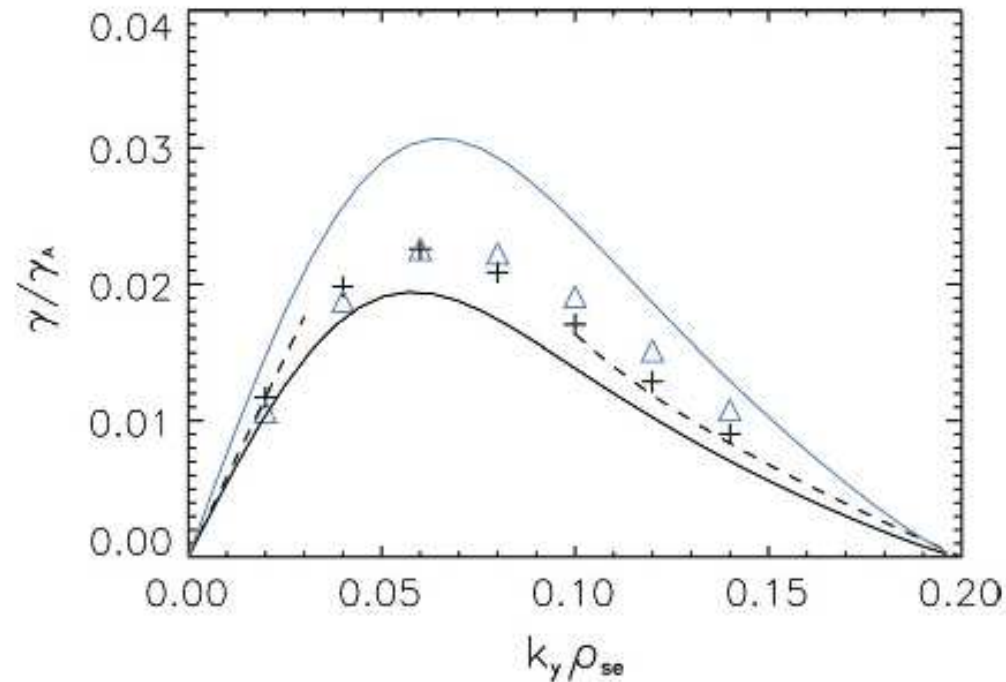
**Case 2** electron scale  $\sim \delta \ll$  ion scale  $\lesssim$  equili. scale

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# Dispersion relation

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Typical form of dispersion relation of tearing instability.



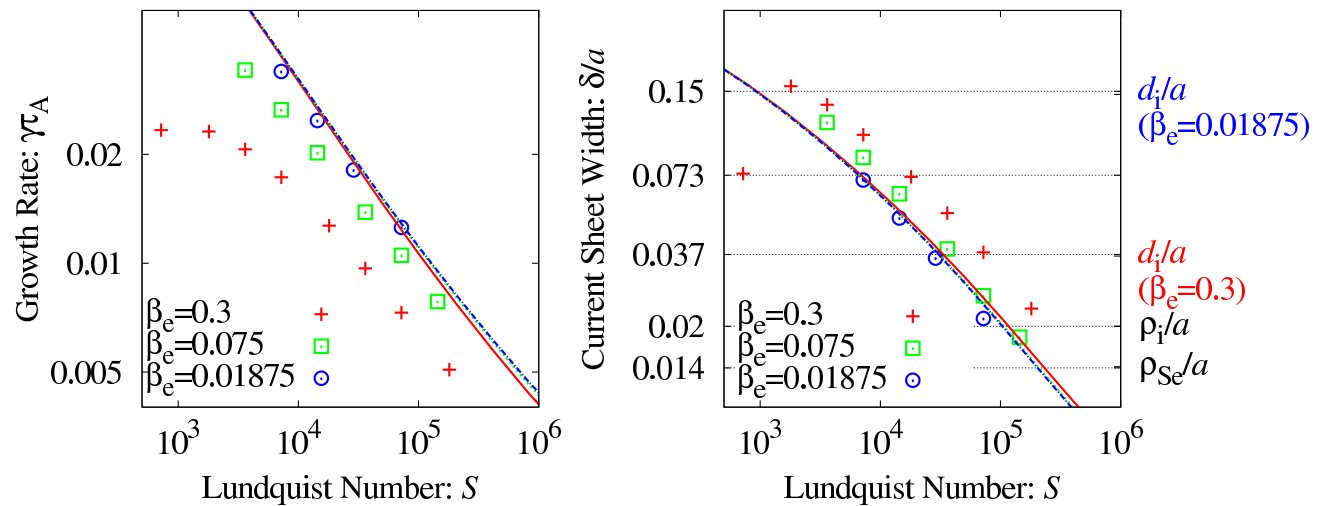
[Fig. taken from Rogers *et al.*, 2011]

$$\begin{aligned} \text{Large } \Delta' & \quad \gamma \tau_A \sim S^{-1/3} \\ \text{Small } \Delta' & \quad \gamma \tau_A \sim S^{-3/5} \end{aligned}$$

# MHD to two-fluid MHD

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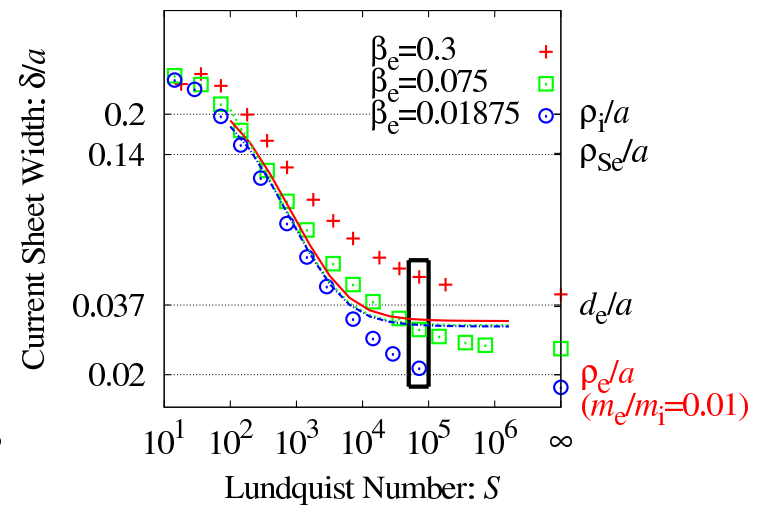
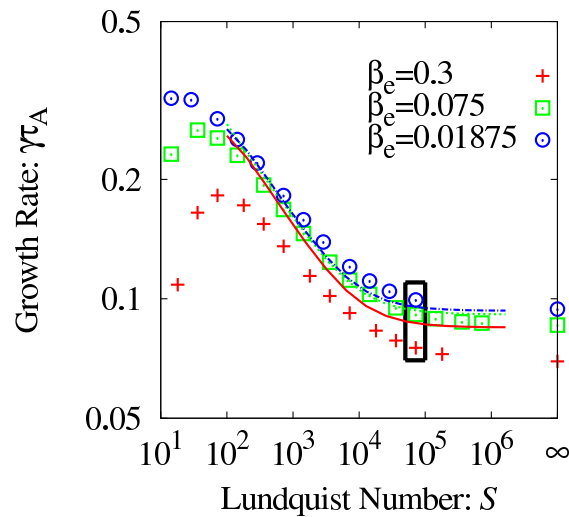
- Growth rate and current layer width scaling against Lundquist number  $S$  are obtained from GK simulation. [dots]
- Scalings are compared with reduced two-fluid model by Fitzpatrick (Fitzpatrick, 2010). [lines]
- GK and 2F results agree well only for low- $\beta_e$ .
- 2F model assumes  $\beta_e \ll \sqrt{m_e/m_i}$ , which is marginally satisfied for  $\beta_e = 0.01875$  case.
- Eqn. of state used in 2F model may not be valid.



# Collisional–collisionless transition

- Collisional–collisionless transitional regime is reproduced:  
For large  $S$ , electron inertia mediates reconnection instead of collisions.

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# Ion temp. dependence: kinetic Alfvén wave

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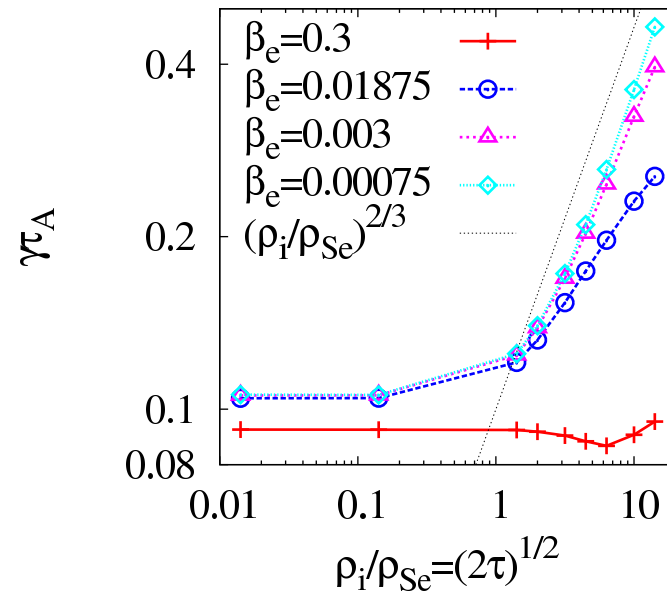
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Summary

- Ion temperature ( $\tau \equiv T_{0i}/T_{0e}$ ) dependence.
- Theoretical prediction,  $\gamma\tau_A \sim \tau^{1/3}$ , because of the transition of Alfvén wave to kinetic Alfvén wave.
- For higher  $\beta_e$ , sound wave couples to Alfvén wave. A compressible effect play a role, and  $\tau^{1/3}$  dependence is no longer seen.



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- We have performed linear GK simulations of tearing instability. It is shown that growth rate scaling with collisionality agrees well with prediction by 2F model only for low beta case.
- For large beta, coupling of Alfvén wave with ion sound wave becomes significant. General non-polytropic equation of state should be considered for pressure perturbations.
- See Numata *et al.*, Phys. Plasmas **18**, 112106 (2011) for more detail.
- Related future works planned: Nonlinear simulations to study kinetic effects on magnetic reconnection, diamagnetic stabilization of tearing instability [@Dartmouth], microtearing turbulence [with Loureiro *et al.*]
- Gyrokinetics is a suitable approach to multiscale kinetic plasmas. AstroGK is a well-established gyrokinetics code. It is free!

